

SOME PETROLOGICAL CONSTRAINS ON THE VESTA MANTLE FROM THE STUDY OF GRAVITATIONAL POTENTIAL BY THE DAWN MISSION. S. A. Voropaev, GEOKHI RAS, Moscow, Kosygina str. 19, 119991 voropaev@geokhi.ru

Introduction: Space mission Dawn targeted 4 Vesta provides a number of remarkable results concerning as surface coverage as physical parameters of the surviving protoplanet. It was confirmed that Vesta differentiated and Rheasilvia, a giant impact basin at the the south polar region, is the most likely source of howardite-eucrite-diogenite (HED) meteorites [1]. But, degree of Vesta’s primary hondritic body melting is not clear till now and depends on the time of its formation at the beginning of the life of the Solar System [2]. So, the core/mantle size and the composition of theirs rocks remains questionable.

Analytical procedure: The Vesta precession rate (due to the gravitational torque from the Sun) and the gravitational potential (modeled by a spherical harmonic expansion) will be determined by unnormalized oblateness J_2 [3]

$$C - (A + B) / 2 = J_2 MR^2,$$

where $A < B < C$ are principal moments of inertia, M is mass, R is the mean radius (adopt value 265 km) and $J_2 = 0.071060892$.

Most recent and relevant data from Dawn are [4] major axes, $a/b/c$ - 286.3/278.6/223.2 (km); mass, M - 2.59076×10^{20} (kg); bulk density, ρ_b - 3456 (kg/m³); rotation rate, ω - 1617.333119 (deg/day).

For our purpose, the shape of Vesta is reasonably well approximated by a twoaxial oblate ellipsoid, $a_1 = b_1 = 282.4$ (km), $c_1 = 223.2$ (km) with hydrostatic structure at first harmonic degree. An exact analytical treatment provides for homogeneous twoaxial oblate ellipsoid (with an arbitrary bulk density)

$$J_2^{(0)} = 1/5 \epsilon_1^2, \text{ where eccentricity } \epsilon_1^2 = 1 - c_1^2/a_1^2.$$

So, for homogenous Vesta, $J_2^{(0)} = 0.075$ ($\epsilon_1 = 0.613$) and $J_2 < J_2^{(0)}$ - indication on the more dense core relative mantle.

In order to explore the implications of the gravity and shape for the interior structure of Vesta, simple two-layer mass-balance model was explored with an assumed core as twoaxial oblate ellipsoid with major axes $a_2 = b_2 > c_2$ and eccentricity $\epsilon_2^2 = 1 - c_2^2/a_2^2$. In this case,

$$M = M_1 + M_2,$$

where $M_1 = 4\pi/3 \rho_1 a_1^2 c_1$, ρ_1 is the mantle’s density, $M_2 = 4\pi/3 (\rho_2 - \rho_1) a_2^2 c_2$, ρ_2 is the core’s density. So, mass-balance provides

$$1 = \rho_1 / \rho_b + (\rho_2 - \rho_1) / \rho_b (a_2/a_1)^2 c_2/c_1$$

or

$$(a_2/a_1)^2 = (\rho_b - \rho_1) / (\rho_2 - \rho_1) \sqrt{1 - \epsilon_1^2} / \sqrt{1 - \epsilon_2^2} \quad (1)$$

For two-layer model an exact analytical treatment provides

$$J_2^{(1)} = 1/5 (M_1/M \epsilon_1^2 + M_2/M \epsilon_2^2 (a_2/a_1)^2) \quad (2)$$

After comparison with (1) we have

$$\epsilon_2^2 / \sqrt{1 - \epsilon_2^2} = (5 J_2^{(1)} - \rho_1 / \rho_b \epsilon_1^2) / \sqrt{1 - \epsilon_1^2} (1 - \rho_1 / \rho_b) (\rho_b - \rho_1) / (\rho_2 - \rho_1) = D1(x, y) > 0, \quad (3)$$

$$x = \rho_1, y = (\rho_2 - \rho_1)$$

We assume that the core’s eccentricity $\epsilon_2 < \epsilon_1$ as for more dense rocks relative mantle. In this case left part of (3) should be less then 0.476. For $J_2^{(1)} = J_2 = 0.071060892$ the right part of the later expression $D1(x, y)$ set limits for the unknown mantle’s density x as shown on Fig.1

$$3.24 < x = \rho_1 < 3.26 \text{ (g/cm}^3\text{)}$$

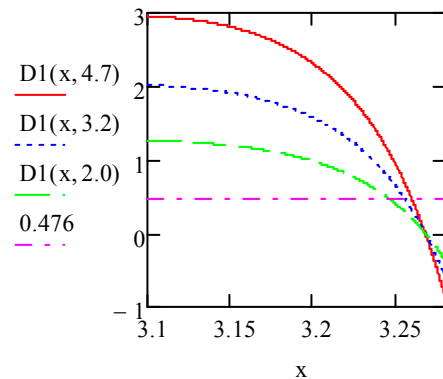


Fig.1

Results and discussion: The above discussed simple core/mantle model provides reasonable value for mean mantle’s density. Diogenites are currently believed to originate from deep within the crust of the Vesta and relatively unbrecciated olivine-rich diogenites consist of an equilibrium assemblage of olivine (3.27-3.37 g/cm³) and magnesian orthopyroxene – harzburgite (2.99-3.2 g/cm³) [5]. So, we can use this model at analytical treatment for more detailed analyses of the gravity of Vesta and implications for internal stresses [6] and hydrostatic equilibrium.

References:

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 [6] S.A. Voropaev (2013), 44th LPSC, Abstract #1135.