

A RHEOLOGICAL, MATHEMATICAL AND STATISTICAL COMPARISON OF LUNAR RILLES AND TERRESTRIAL LAVA TUBES. Sonit Sisolekar¹, Raymond Duraiswami¹, Aristotle Monterio¹. ¹Department of Geology, Savitribai Phule Pune University, Pune - 411007 India

Introduction: The rheological characteristics of lunar lava flows are yet to be fully understood. Mathematical analysis of lunar rilles (LRs) can be helpful in deriving these. This study compared the dimensions and other rheological parameters of lunar and terrestrial lava tubes. There were some successful attempts at finding the reason behind the huge dimensions of lunar rilles, and the existence of lava channels/tubes as rilles. It was concluded that the eruption temperatures of lunar lavas were relatively very high, allowing them to flow for longer distances; the low atmospheric pressure and gravity led to more inflation, and thus to deeper and wider flows.

Data and Methods: In this study, the data from Hurwitz et. al. [1] was used to study the lunar rilles; while the ASU (Arizona State University) worldwide lava-tube database revealed the dimensions of terrestrial lava-tubes. The dimensions and floor-slope were used to find out various parameters like viscosity, effusion rate, etc. using various equations [2], [3], [4], [5], [6] and [7]. The results are given in Table 1.

Results and Discussion:

1] It was observed that the length, width and depth of lunar rilles is very high as compared to the lava-tubes on Earth. The length of lunar rilles, for instance, was 85-88 times more than terrestrial ones. This may indicate 2 things - a) The lunar lavas were hotter than terrestrial lavas; and b) The total mass of lava erupted was much more than on the Earth. To check this, the SiO₂ and MgO contents were compared. It is known that higher the SiO₂ content and lower the MgO content, the lower is the temperature of the lava. It was found that average SiO₂ was lower (45.4 wt%) and average MgO higher (9.24 wt%) on the Moon [8] [9]. This implies that lunar lava was hotter and took a longer time to cool, thus leading to the formation of longer lava flows.

2] It was evident through calculations that the basal stress in case of lunar rilles is 50% more than that of terrestrial lava-tubes. This leads to 2 inferences: a) the basal stress is higher because the flow depth is higher on the Moon; and b) lunar lava-tubes have more erosive power: their huge basal stress indicates high substrate erosion, and loss of energy in displacing substrate debris. Thus, the lava flows/channels form rilles later on.

3] Average total lava mass of the lunar rilles is observed to be 4764 times that of terrestrial ones. This

is the parameter which differs the most between the lunar rilles and the terrestrial lava-tubes.

4] Average aspect ratio (AR) of the lunar rilles is observed to be 4.2 times that of terrestrial ones. This implies that inflation happens more vigorously in case of lunar lava flows. Since atmospheric pressure and gravity is less on the Moon, the lava flows are relatively free to inflate to a larger extent. Thus, it can be inferred from the above explanations that AR is a function of both atmospheric pressure and gravity. This also explains why vesicularity is significantly negligible in lunar basalt as observed in the samples from Apollo missions. Due to less atmospheric pressure at the time of eruption, the degassing of volatiles took place immediately and lost to the dissipating lunar atmosphere.

5] Average yield strength of the lunar rilles is observed to be half that of terrestrial ones. This means that the lunar lavas were less viscous compared to the terrestrial lavas. This reconfirms that the lunar lavas were hotter at the time of eruption, thereby having lesser yield strength. In addition, the low stress may signify that they are less vesicular, since it is often associated with high viscosity and/or yield strength.

6] The viscosity was calculated to check the validity of the above argument and was found to be 460 times less on the Moon, indicating the argument to be valid. This could suggest that the lunar magmas didn't experience heat loss and assimilation of the wall rock in the magmatic plumbing system or while ascending the crust. One possible explanation could be due to the fact that the Moon's crust is definitely very thin when compared to that of the Earth.

7] When 'total lava-tube mass'(mlt) is plotted against 'erupted mass'(me), the trend-slope is found to be higher in the graph for the LR's (Figure 1). in comparison to lava tubes on Earth (Figure 2). This implies that, compared to the Earth, the lunar rilles consist of a huge portion of the total erupted mass of lava. In other words, the LR's are more efficiently formed than terrestrial lava-tubes.

References: [1] Hurwitz et al. (2013) Planet. Space Sci., 79–80, 1-38. [2] Moore (1987) USGS Prof Paper 1350:1569-1588. [3] Cattermole (1996) J Wiley & Sons, London. [4] Sparks et al. (1976) Geology 4: 269-271. [5] Hulme (1974) Geophys. J R Astr Soc 39: 361-383. [6] Pinkerton and Wilson (1994) Bull Volcanol 56: 108-120. [7] Chester e al. (1985) Chapman and hall, London 187-227. [8] Taylor and Stuart (1975)

Pergamon Press, New York. [9] Philpotts and Ague (2009) Cambridge University Press.

Table 1. Basic statistics of various parameters of lunar LRs and terrestrial lava-tubes, and their comparison.

| PARAMETRES | unit | Dimensions | | | Slope deg | de (equivalent c Time | | Velocity m/s |
|----------------------------------|--------------------|------------|--------|--------|-----------|-----------------------|-------------|--------------|
| | | length | width | depth | | m² | hours | |
| EARTH(E) | AVERAGE | 777.31 | 9.88 | 4.67 | 9.44 | 2.36 | 364.23 | 0.08 |
| | Maximum | 65500 | 200 | 20 | 30 | 4 | 833.33 | 5.24 |
| | Minimum | 3 | 0.91 | 0.6 | 0.3 | 0.63 | 20.67 | 0.00006 |
| | Standard Deviation | 3053.24 | 41.98 | 12.18 | 78.6 | 1.16 | 301.68 | 0.22 |
| MOON(M) | AVERAGE | 66758.43 | 628.69 | 70.54 | 0.35 | 3.34 | 59899831.95 | 0.0000198 |
| | Maximum | 565680 | 4270 | 534.36 | 1.4 | 3.85 | 78987496.71 | 0.00073 |
| | Minimum | 2130 | 160 | 4.22 | 0.01 | 2.57 | 35278567.5 | 0.0000078 |
| | Standard Deviation | 86442.88 | 573.73 | 78.71 | 0.33 | 0.26 | 9230918.53 | 0.000026 |
| Average (moon) / Average (earth) | | | | | | | | |
| [AE/AM ratio] | | 85.88 | 63.65 | 15.12 | 0.04 | 1.41 | 2740.93 | 0.00024 |

| Mass Flux kg/s | Basal Stress kg/m/s | Lava-Tube Mass kg | Aspect Ratio dimensionless r | Yield Strength N/m² | Viscosity kg/m/s | W0 (levee width) m | E (Effusion rate) m | m _e Celcius |
|----------------|---------------------|-------------------|------------------------------|---------------------|------------------|--------------------|---------------------|------------------------|
| 115477.36 | 10142.81 | 3509916287 | 2.12 | 88381.5 | 1.57257E+24 | 10.53144498 | 30.24219712 | 483577644.7 |
| 12140352 | 74823.21 | 421540000000 | 10 | 956052.72 | 4.36974E+25 | 82.7533439 | 739.1112911 | 11456225012 |
| 4.46 | 695.23 | 35181.73 | 1.52 | 1327.85 | 2.43709E+15 | 0.6750832833 | 0.03758263382 | 962959.1176 |
| 3130636.19 | 12060.88 | 108763574838 | 3.45 | 78681.18 | 8.80175E+23 | 11.83264683 | 15.91410138 | 249444998.1 |
| 5519.96 | 15268.34 | 16721706764931 | 12.69 | 41512.28 | 3.4228E+21 | 16.15454884 | 2.032568243 | 1799050858679 |
| 13795.21 | 17121.99 | 1.11857E+15 | 50.77 | 343504.8 | 0.01884927684 | 248.8406598 | 124.7833847 | 1.14028E+15 |
| 9.77 | 73.16 | 44697049920 | 3.6 | 418.4 | 46065680.88 | 0.07665000117 | 0.003524044161 | 44833339641 |
| 25406.36 | 30978.59 | 80380705745556 | 7.46 | 57887.96 | 3.45529E+22 | 32.58471913 | 9.301740871 | 8396265309795 |
| 0.048 | 1.51 | 4764.13 | 5.99 | 0.51 | 0.0022 | 1.53 | 0.07 | 37202.94 |

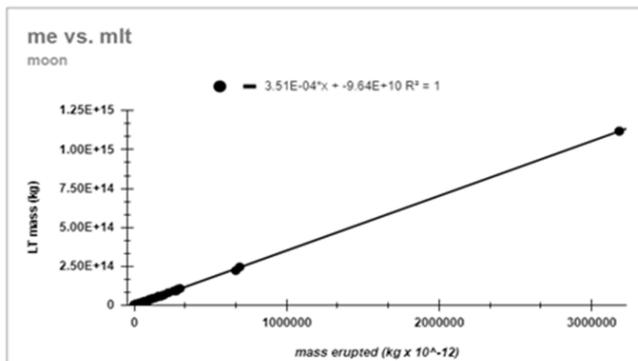


Figure 1. Lava-tube mass [LT mass] against erupted mass, for lunar rilles (n=190 rilles). The relation is found to be:
 $m_{lt} = 0.000351m_e - (9.64 \times 10^{10})$
 $R^2 = 1$

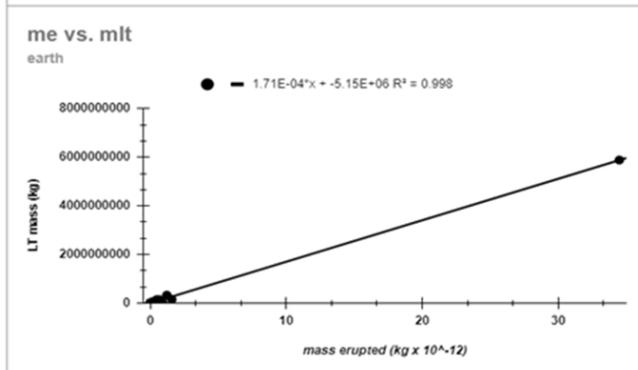


Figure 2. Lava-tube mass [LT mass] against erupted mass, for terrestrial lava-tubes (n=30 lava-tubes). The relation is found to be:
 $m_{lt} = 0.000171m_e - 5150000$
 $R^2 = 0.998 = (\sim 1)$