

**FORECASTING FOR THE HAZARDOUS ASTEROIDS APPEARANCE.** N. I. Perov<sup>1,2</sup>. <sup>1</sup>State Autonomous Cultural and Education Organization named after V.V. Tereshkova. 150000, Yaroslavl, Ul. Chaikovskogo, 3, Russian Federation. E-mail: [perov@yarplaneta.ru](mailto:perov@yarplaneta.ru). <sup>2</sup>State Pedagogical University named after K.D. Ushinskii. 150000, Yaroslavl, Ul. Respublikanskaya, 108, Russian Federation.

**Introduction:** For unperturbed motion of the Solar system's bodies there is collection of modes for the determination of epochs, corresponded for the minimal distances between the two bodies [2]. These arbitrary unperturbed trajectories may be determined, for example, from optical observations with using one and the same algorithm without singularities [3].

Below in the frame of the pairwise two body problem ("the Sun and a particle" and "the Sun and the Earth"), with taking into account the motion of line of apsides and line of nodes [1], the minimal distance between the Earth and a small body is determined.

**The Based Equations:** Let's denote  $a_1, a_2$  are the semimajor axes of the orbits of the Earth and the asteroid;  $e_1, e_2$  are the eccentricities of the considered orbits;  $i_1, i_2$  are the inclinations of the orbital planes in respect of the ecliptic plane for the given epoch;  $\omega_1, \omega_2$  are the arguments of the perihelia of the Earth and the asteroids;  $\Omega_1, \Omega_2$  are the longitudes of the ascending nodes of the considered planes;  $v_1, v_2$  are the true anomalies of the bodies [1], [4], [5].

The relationship for searching of minimal distance  $r_{12}$  between the Earth and the small body we represent in the form (1)

$$r_{12}^2 = (\mathbf{r}_1 - \mathbf{r}_2)^2 = \min. \quad (1)$$

Here,  $\mathbf{r}_1$  and  $\mathbf{r}_2$  – the heliocentric vectors of the positions of the Earth and the asteroid.

In line with the theory [1], the following assumptions were made.

$$r_1 = \frac{p_1}{1 + e_1 \cos(v_1)}, \quad (2)$$

$$p_1 = a_1(1 - e_1^2), \quad (3)$$

$$x_1 = r_1(\cos(v_1 + \omega_1) \cdot \cos(\Omega_1) - \sin(v_1 + \omega_1) \cdot \sin(\Omega_1) \cdot \cos(i_1)), \quad (4)$$

$$y_1 = r_1(\cos(v_1 + \omega_1) \cdot \sin(\Omega_1) + \sin(v_1 + \omega_1) \cdot \cos(\Omega_1) \cdot \cos(i_1)), \quad (5)$$

$$z_1 = r_1(\sin(v_1 + \omega_1) \cdot \sin(i_1)). \quad (6)$$

The same equations (2)–(6) we put for the second body, using index "2".

In order to take into account the variations of the quantities of  $\omega_1, \omega_2, \Omega_1, \Omega_2$ , we represent these parameters in the forms

$$\omega_1 = \omega_{10} + k_1 d_1, \quad (7)$$

$$\omega_2 = \omega_{20} + k_2 d_2, \quad (8)$$

$$\Omega_1 = \Omega_{10} + K_1 d_1, \quad (9)$$

$$\Omega_2 = \Omega_{20} + K_2 d_2. \quad (10)$$

Here  $k_1, k_2, K_1, K_2$  are empirical constants.  $d_1, d_2$  are variable values, with imposed a constraint on the ascending nodes (The closest approaching of the considered bodies takes place in the ascending nodes, which are equal).

$$\Omega_1 = \Omega_2, \quad (11)$$

or

$$d_2 = (\Omega_{10} + K_1 d_1 - \Omega_{20}) / K_2. \quad (12)$$

The index "0" references to the initial data sets of  $\omega_1, \omega_2, \Omega_1, \Omega_2$ .

The quantities of  $r_{12}, x, y, z$ , and the first derivatives we find with using equalities (1) – (12) and the based equations we write as (13)

$$\begin{aligned} \frac{dr_{12}}{dv_1} &= 0; \\ \frac{dr_{12}}{dv_2} &= 0; \\ \frac{dr_{12}}{dd_1} &= 0. \end{aligned} \quad (13)$$

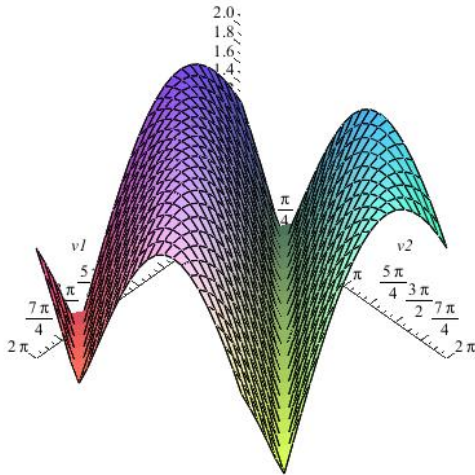
For the process of calculating we use the system "MAPLE'15".

**Example:** Let's find the numerical values of  $v_1, v_2$ , and  $d_1$  for the epoch of the Earth and the asteroid 2019 SU3 approaching. The initial orbital elements for the Earth and the asteroids are referred to the date 27, April, 2019 [1], [4], [5]. The unit of length is 1 AU. We put mass of the asteroid is less than mass of the Earth.

Using the empirical relation of  $\omega$  to  $\Omega$  for the planets of the Solar system [1] we may eliminate some singularities for the computations (for instance, if resonance in motion of the bodies is possible). So, put

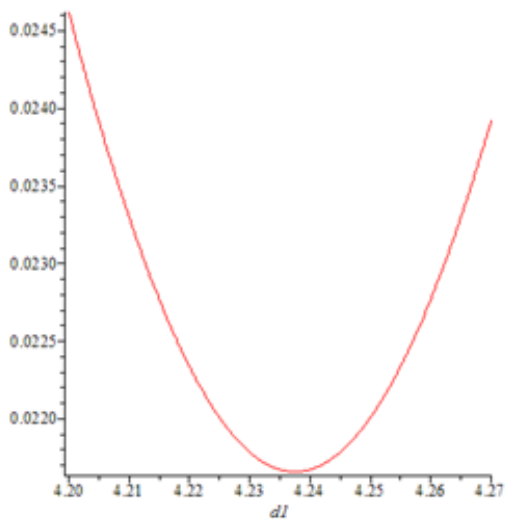
$$k_1 = \sqrt{2}, K_1 = -1, k_2 = \sqrt{3}, K_2 = -1. \quad (14)$$

Numerical and analytical investigations of two body's motion along heliocentric orbits in the interval of the several revolutions show there are local and global minimums of the distance  $r_{12}$  between the bodies. (**Fig. 1**).



**Fig.1.** The distance  $r_{12}=r_{12}(v_1, v_2)$  between the Earth and the asteroid 2019 SU3 is measured in AU.  $d_1=0.0173501769$  rad. The true anomalies  $v_1$  и  $v_2$  take values in the interval from 0 to  $2\pi$  rad.

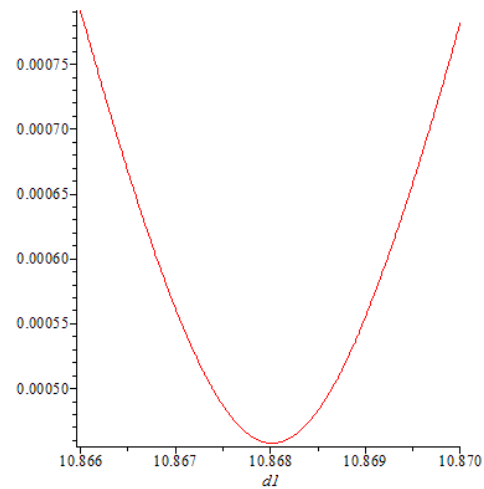
The formulae (1) – (13) permit to determine the distance  $r_{12}$ , and plot the graph of the function  $r_{12}=r_{12}(d_1)$ . (**Fig. 2**), (**Fig. 3**).



**Fig.2.** One of the local minimums of the functions  $r_{12}$  is the distance  $r_{12}=r_{12}(d_1)$  between the Earth and the asteroid 2019 SU3 is measured in AU.  $d_1$  is measured in rad.  $v_1=0.05981311596$  rad,  $v_2=0.008946200265$  rad.

**Conclusion:** The advanced way gives scope for take into account the motion of perihelia and ascending nodes of celestial bodies. Estimation of the perturbations offers to determine the global minimum of  $r_{12}$

between the Earth and the hazardous bodies with the smaller error (**Fig. 3**).



**Fig.3.** The global minimum of the function  $r_{12}$  ( $r_{12}$  is the distance between the Earth and the asteroid 2019 SU3 measured in AU).  $d_1$  is measured in radians.  $v_1=1.6822015501976$  rad,  $v_2=5.807095699091$  rad.

**References:** [1] Roy A.E. (1978) *Orbital Motion*. Adam Hilger. Bristol. [2] Perov N. I. (2000) *Solar System Research*, 2000. V. 34. N. 1. P. 95. URL: <https://ui.adsabs.harvard.edu/abs/2000SoSyR..34...95P> [3] Perov N. I. (1989) *Astronomicheskii Zhurnal*, 1989. V. 66. P. 1093-1099. URL: <https://ui.adsabs.harvard.edu/abs/1989AZh....66.1093P>. [4] 2019 SU3 - Wikipedia. URL: [https://en.wikipedia.org/wiki/2019\\_SU3](https://en.wikipedia.org/wiki/2019_SU3). [5] Sentry (monitoring system). URL: [https://en.wikipedia.org/wiki/Sentry\\_\(monitoring\\_system\)](https://en.wikipedia.org/wiki/Sentry_(monitoring_system)). [6] Murray C.D. and Dermott S.F. (2009) *Solar System Dynamics*. Cambridge University Press.