Mass of Kepler Exoplanet Candidates and Benford's Law of First Digits. Thomas W. Hair (twhair@fgcu.edu), Florida Gulf Coast University, 10501 FGCU Blvd., Fort Myers, Florida 33965.


#### Abstract

Benford's Law refers to the frequency distribution of the first digits found in many natural and human-constructed sources of data. In this distribution, the number 1 occurs as the leading digit approximately $30 \%$ of the time, while larger numbers occur in that position with decreasing frequency. This distribution of first digits is the same as the widths of gridlines on a logarithmic scale and its results have been applied to a wide variety of data sets. From pulsar rotation rates to accounting fraud detection, this distribution tends to be most accurate when values within the data set are distributed across multiple orders of magnitude.

Kepler Space Telescope exoplanet mass data, both confirmed and candidate exoplanets, from the Exoplanet Orbit Database are analyzed for goodness-offit with the predicted distribution of the first digits implied by Benford's Law. The surprisingly close match between the confirmed exoplanets and Benford's distribution suggests a limited predictive ability for the mass distribution of exoplanets while a similarly close match of exoplanet candidates provides further evidence that the majority of these candidates, in fact, represent actual exoplanets.


References: [1] Benford, F. (1938) The law of anomalous numbers, Proceedings of the American Philosophical Society, 78(4), 551-572.
[2] Duncan, R. (1967) An application of uniform distribution to the Fibonacci Numbers, The Fibonacci Quarterly, 5, 137-140.
[3] Hill, T. P. (1995a) The significant digit phenomenon, American Mathematical Monthly, 102, 322-327.
[4] Hill, T. P. (1995b) Base invariance implies Benford's law, Proceedings of the American Mathematical Society, 123, 887-895.
[5] Hill, T. P. (1995c) A statistical derivation of the significant digit law, Statistical Science, 10, 354-363. [6] Hill, T. P. (1998) The first digit phenomenon, American Science, 86, 358-363.
[7] Ley, E. (1996) On the peculiar distribution of the U.S. stock indexes' digits, American Statistics, 50, 311-314.
[8] Manchester, R., Hobbs, G., Teoh, A., and Hobbs, M. (2005) The Australian telescope national pulsar catalogue, Astrophysics Journal, 129, 1993-2006. [9] Newcomb, S. (1881) Note on the frequency of use of the different digits in natural numbers, American Journal of Mathematics, 4-1, 39-40.
[10] Nigrini, M. (1996) A taxpayer compliance application of Benford's law, Journal of the American Tax Association, 18, 72-91.
[11] Wright, J., Marcy, G. Exoplanet Orbit Database, California Planet Survey, 2013
[12] Sambridge, Tkalcic, and Jackson (2010) Benford's law in the natural sciences, Geophysical Research Letters, Nov 2010.
[13] Schneider, J. (1999) The study of extrasolar planets: methods of detection, first discoveries, and future perspectives, C. R. Acad. Sci. Paris, 327, 621.

